

$$A_{i+1} = -\frac{(2M-kV_0-iM)A_i+kMA_{i-1}}{(i+1)V_0} \quad \text{for } i \geq 2. \quad (41)$$

Integration by parts suggests that

$$A_0 = 0, A_1 = 1, A_2 = 0, \text{ and } A_3 = -kM/3V_0. \quad (42)$$

Expanding Eq. (40) to obtain the first three terms and using the results from Eqs. (32) and (42), the solution becomes

$$P_S = P_H + Ae^{ka} + \frac{C^2}{(V_0 - Ma)^2} \sum_{i=3}^{\infty} A_i a^i. \quad (43)$$

The constant of integration A is determined from the point at which the Hugoniot and the isentrope curves cross. Here $P_S = P_H$ and $a = a_H$ so that

$$P_H = P_H + Ae^{ka_H} + \frac{C^2}{(V_0 - Ma_H)^2} \sum_{i=3}^{\infty} A_i a_H^i$$

and

$$A = -\frac{C^2 e^{-ka_H}}{(V_0 - Ma_H)^2} \sum_{i=3}^{\infty} A_i a_H^i. \quad (44)$$

From Eq. (43), the pressure in terms of a anywhere along an isentrope can be calculated since the A_i 's are determined from Eq. (41), A is found from Eq. (44), and P_H and a_H are experimentally determined values.

The calculation of an isotherm is very similar. Starting again with Eq. (24)

$$P_T - P_H = \Gamma/V(E_T - E_H) \quad (45)$$

where P_T and E_T are the pressure and energy along an isotherm.

Differentiating Eq. (45) with respect to volume yields

$$\left(\frac{\partial P}{\partial V}\right)_T - k\left(\frac{\partial E}{\partial V}\right)_T = \left(\frac{\partial P}{\partial V}\right)_H - k\left(\frac{\partial E}{\partial V}\right)_H \quad (46)$$

which represents the differential equation for pressure along an isotherm. At this point, it becomes advantageous to express $(\partial E/\partial V)_T$